

Combining Models of Physical Effects for Describing Complex Electromechanical Devices

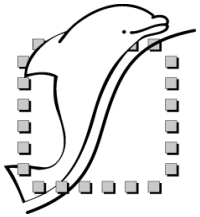
Lars M. Voßkämper

Dolphin Integration GmbH

Gerhard Mercator University Duisburg

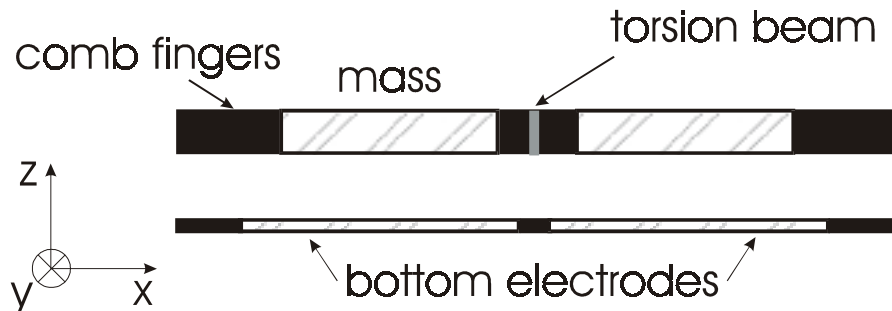
Outline

- ◆ Demonstrator: gyroscope
- ◆ Basic effects occurring in the gyroscope
- ◆ Implementation in VHDL-AMS
- ◆ Object models created with basic effects
- ◆ Device modeling and simulation
- ◆ System modeling and simulation
- ◆ Conclusion



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Side View:



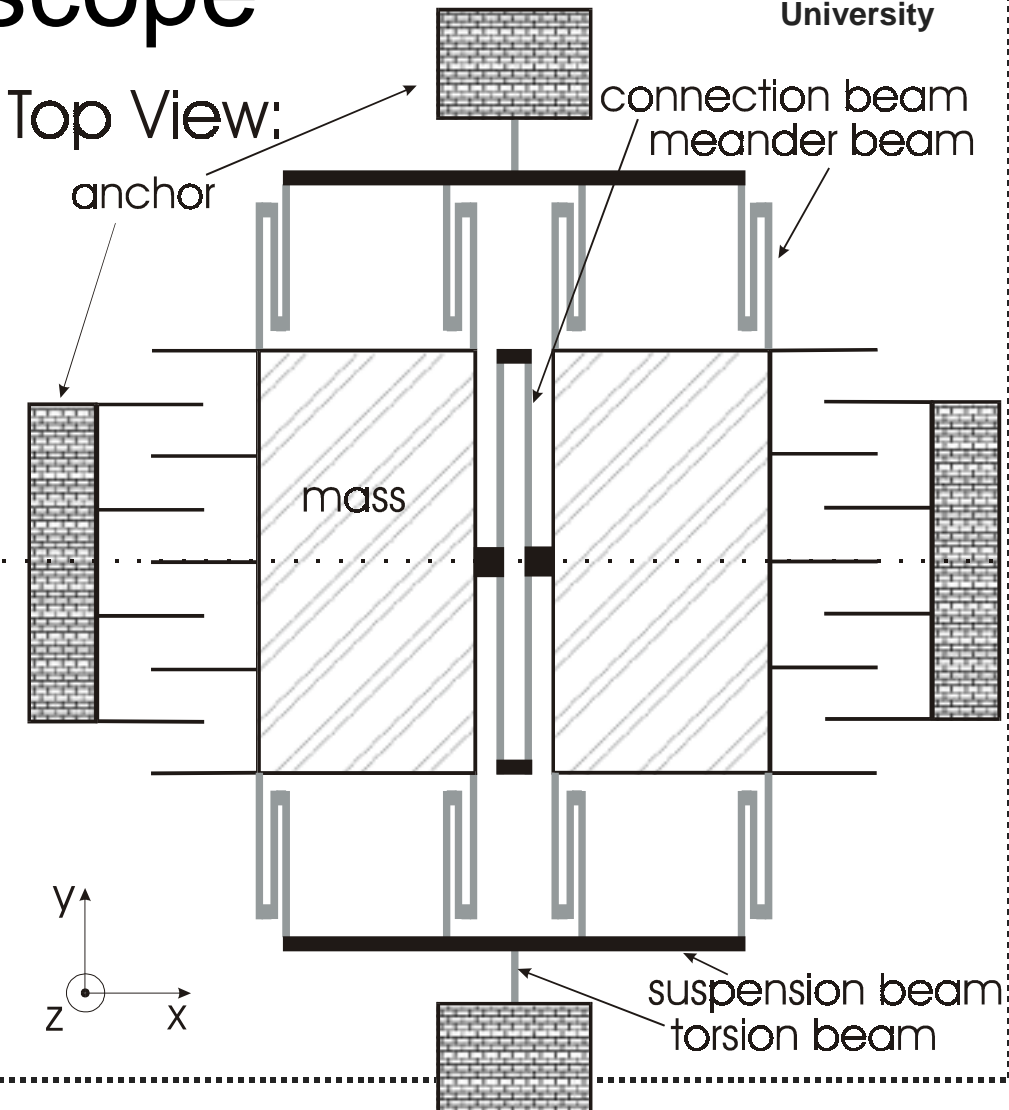
- ♦ opposite in phase motion of masses
- ♦ angular velocity induces tilting of masses
- ♦ detection due to capacity difference

Demonstrator: Gyroscope



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Top View:



Basic Effects Occurring in the Gyroscope

- ◆ Bending and torsion effects of beams
- ◆ Translational and rotational inertia effects
- ◆ Air damping effects
- ◆ Capacity effect between two conductive plates
- ◆ Attraction effect of two conductive plates
- ◆ Coriolis effect

Analytical Modeling of Basic Effects

Port definition to make models compatible with each other

type of variable	electrical network	rotational movement	translational movement
"through"- variable	current i	torque T	force F
"across"- variable	voltage v	angle φ angular velocity ω	displacement x velocity v

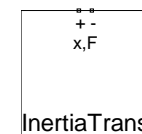
Effect

Equation

Symbol

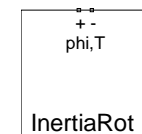
translational inertia effect of masses

$$F = -m \frac{d^2}{dt^2} x$$



rotational inertia effect of masses

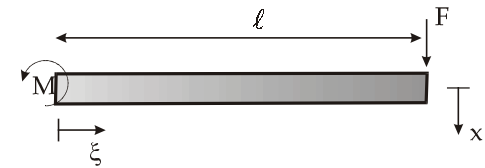
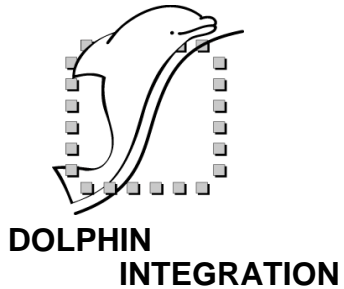
$$T = -J_A \frac{d^2}{dt^2} \varphi$$





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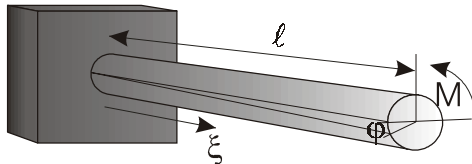
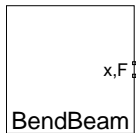
Analytical Modeling of Basic Effects



bending effect of beams

$$\frac{d^2 x_{(\xi)}}{d\xi^2} = -\frac{M_{(\xi)}}{EI_{(\xi)}}$$

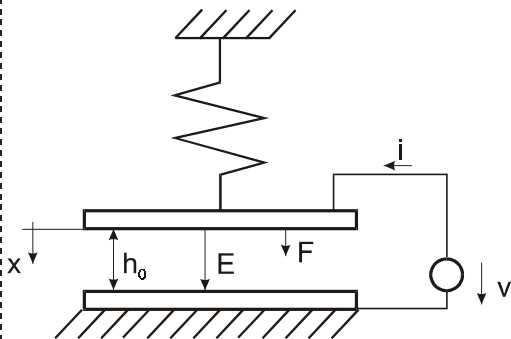
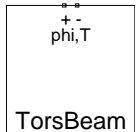
$$\Rightarrow F = \frac{3EI}{l^3} x$$



torsion effect of beams

$$\frac{d\varphi_{(\xi)}}{d\xi} = \frac{T_{(\xi)}}{GI}$$

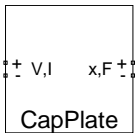
$$\Rightarrow T = \frac{GI}{l} \varphi$$



capacity effect between
two conductive plates

$$C_{(x)} = \varepsilon \frac{A}{h_0 - x}$$

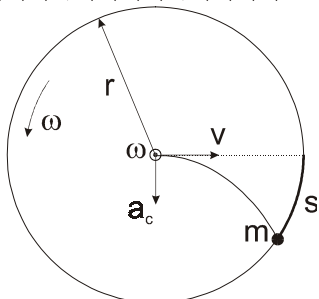
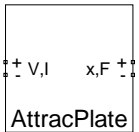
$$\Rightarrow i = C_{(x)} \frac{d}{dt} v$$



attraction effect between
conductive plates

$$\vec{F} = \frac{dE}{d\vec{x}}$$

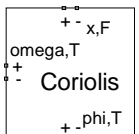
$$\Rightarrow F_x = \frac{1}{2} \varepsilon A \frac{v^2}{(h_0 - x)^2}$$

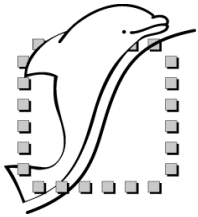


Coriolis effect

$$\vec{T} = 2 \cdot m \cdot \vec{r} \times (\vec{v} \times \vec{\omega})$$

$$\Rightarrow T = 2m\omega x \frac{d}{dt} x$$



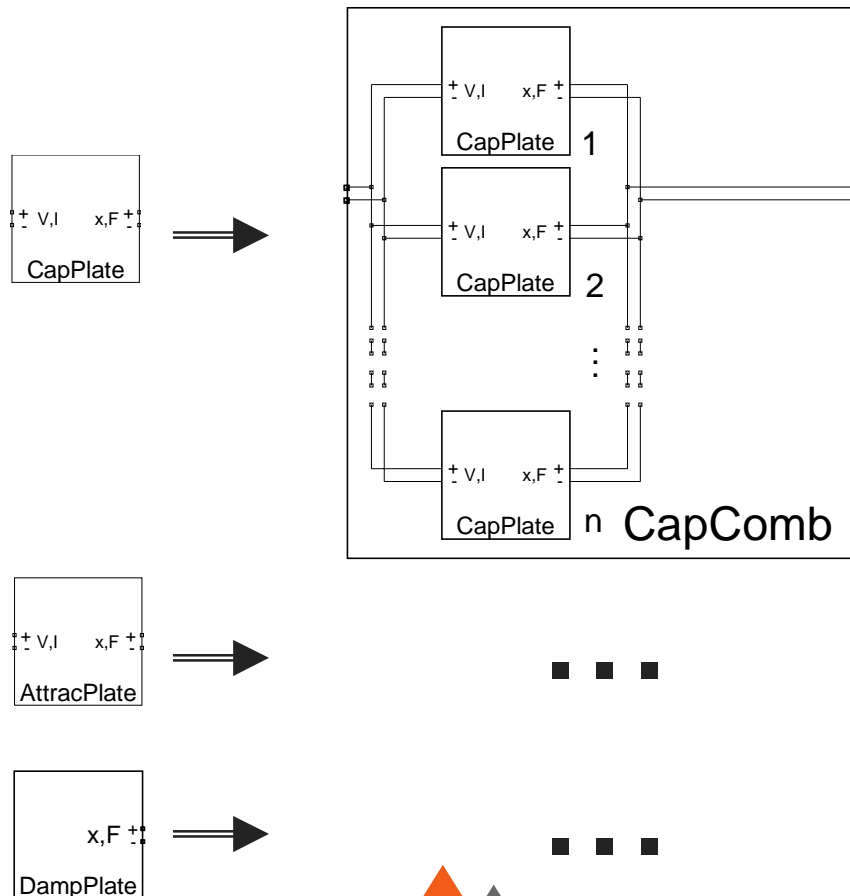


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Object Models Created with Basic Effects

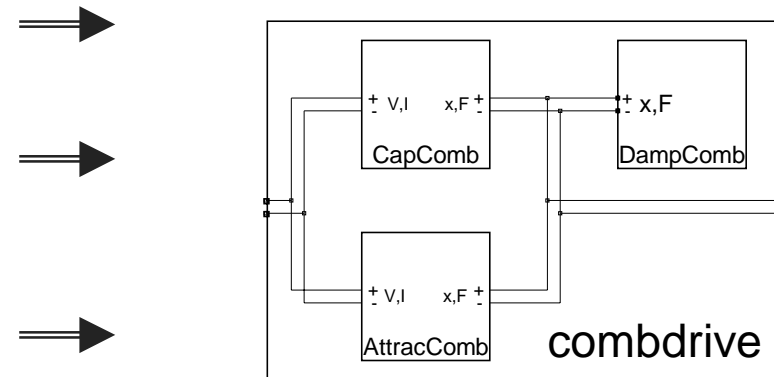


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Modeling a comb drive out of basic effects:

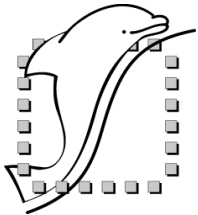
- ◆ capacity effect between plates
- ◆ attraction effect between plates
- ◆ damping effect of moving plates



Implementation in VHDL-AMS

```
01: PACKAGE translational_system IS
02:   ATTRIBUTE unit : string;
03:   -- Displacement in meter
04:   SUBTYPE displacement IS REAL TOLERANCE "default_displacement";
05:   ATTRIBUTE unit OF displacement : SUBTYPE IS "m";
06:   -- Velocity in meter/second
07:   SUBTYPE velocity IS REAL TOLERANCE "default_velocity";
08:   ATTRIBUTE unit OF velocity : SUBTYPE IS "m/s";
09:   -- Force in newton
10:   SUBTYPE force IS REAL TOLERANCE "default_force";
11:   ATTRIBUTE unit OF force : SUBTYPE IS "N";
12:   -- Translational Natures
13:   NATURE translational IS
14:     displacement ACROSS
15:     force THROUGH
16:     translational_ref REFERENCE;
17: END PACKAGE translational_system;
```

Extract from the implementation of
variables types used in translational system

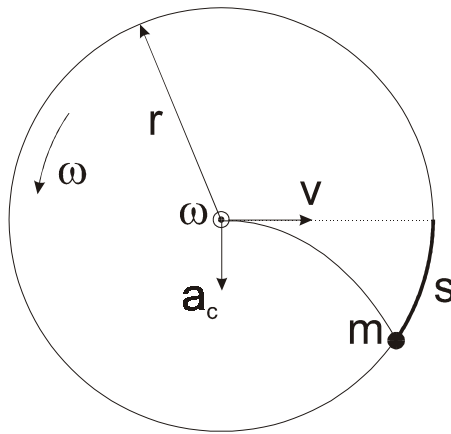


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Implementation in VHDL-AMS



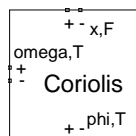
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Coriolis acceleration $\vec{a}_c = 2\vec{v} \times \vec{\omega}$

Coriolis force $\vec{F}_c = 2m\vec{v} \times \vec{\omega}$

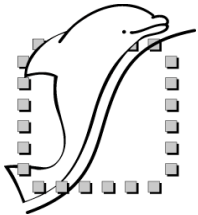
Coriolis torque $\vec{T} = 2 \cdot m \cdot \vec{r} \times (\vec{v} \times \vec{\omega})$



$$T = 2m\omega x \frac{d}{dt} x$$

```
01: USE work.translational_system.all;
02: USE work.rotational_system.all;
03:
04: ENTITY Coriolis IS
05:   GENERIC (width, length, depth : REAL;
06:            roh : REAL := 2.32e3);
07:   PORT (TERMINAL trans_p, trans_n : TRANSLATIONAL;
08:         TERMINAL rot_p, rot_n : ROTATIONAL;
09:         TERMINAL rot_om_p, rot_om_n : ROTATIONAL_OMEGA);
10: END ENTITY Coriolis;
11:
12: ARCHITECTURE simple OF Coriolis IS
13:   QUANTITY pos ACROSS trans_p TO trans_n;
14:   QUANTITY torque THROUGH rot_p TO rot_n;
15:   QUANTITY omega ACROSS rot_om_p TO rot_om_n;
16:   CONSTANT mass : REAL := width*length*depth*roh;
17: BEGIN
18:   torque == 2.0 * mass * omega * pos * pos'dot;
19: END ARCHITECTURE simple;
```

Implementation of Coriolis effect

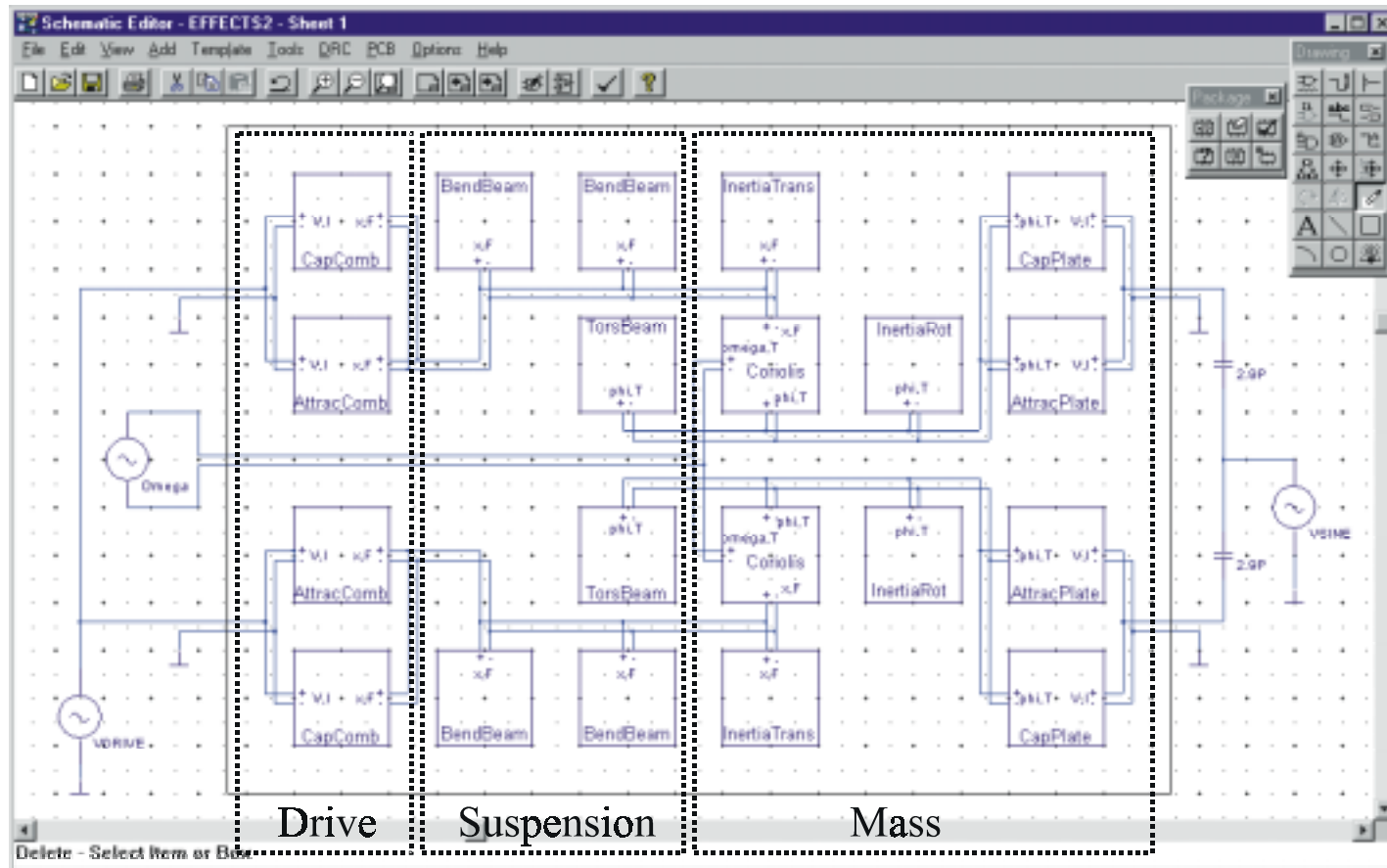


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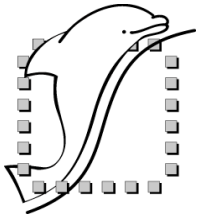
Device Modeling



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Gyroscope's netlist with basic testbench for device simulation

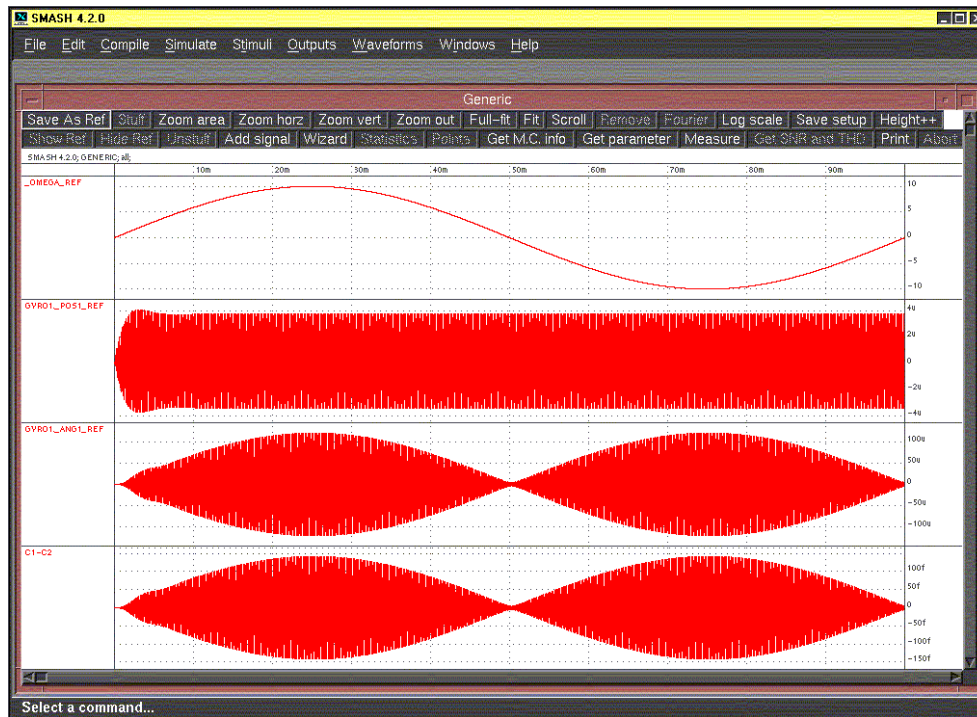


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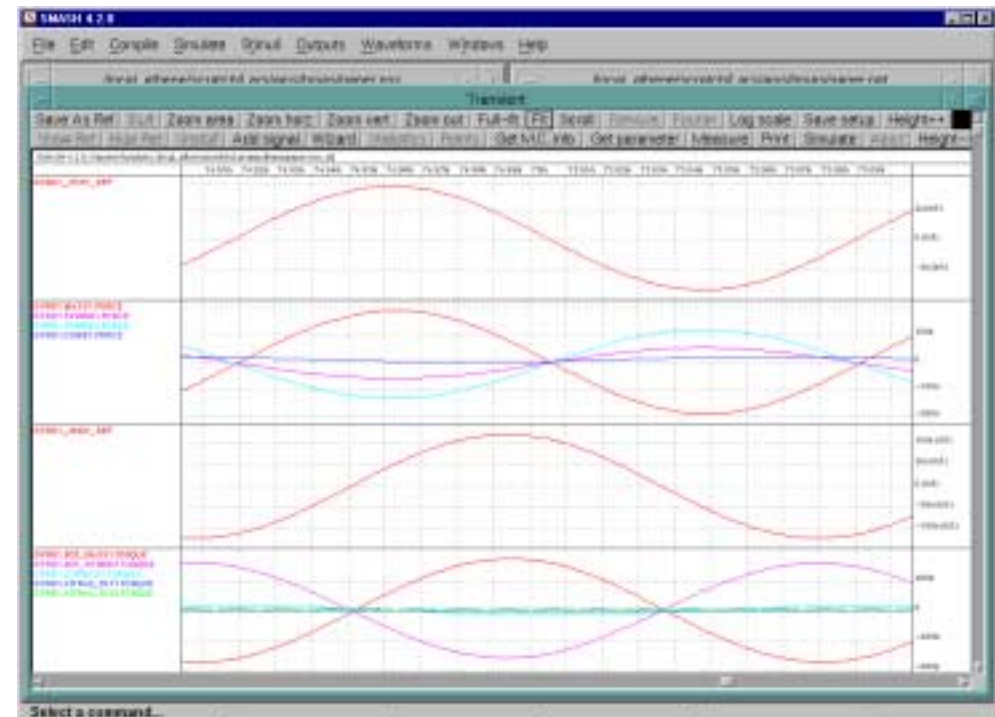
Device Simulation



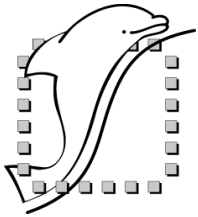
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angular velocity, displacement, tilt angle
and capacity difference



displacement, forces, tilt angle
and torques

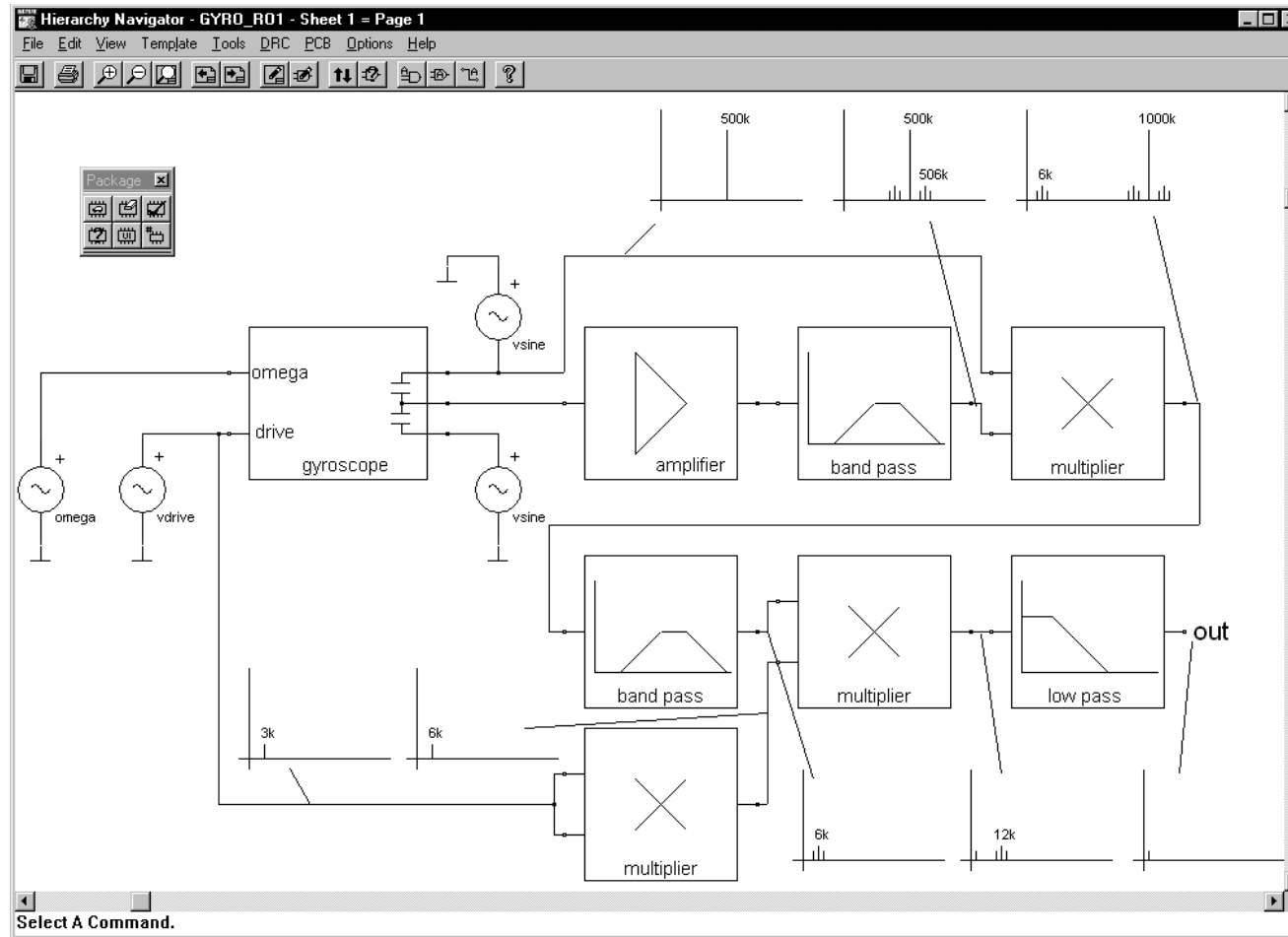


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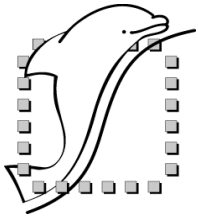
System Modeling



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Functional view of the gyroscope readout circuit

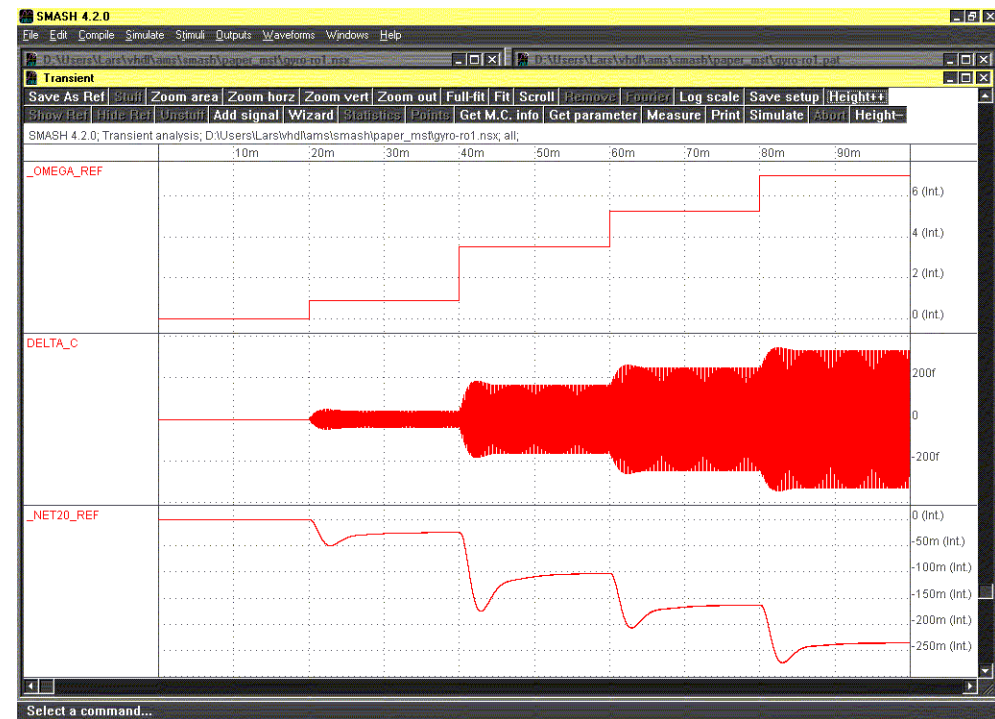
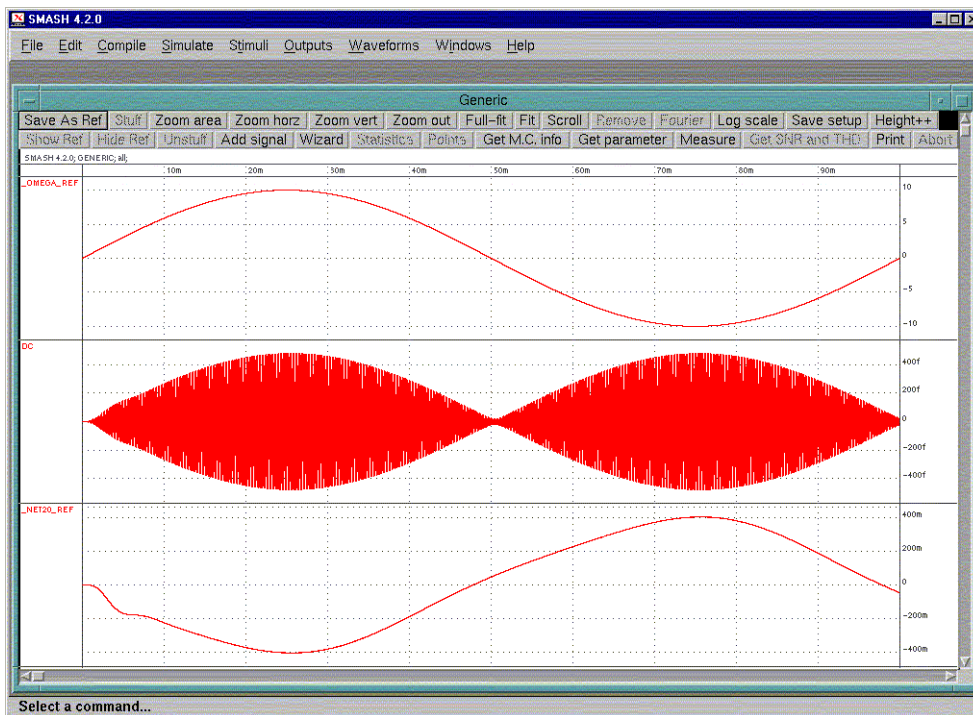


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System Simulation



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angular velocity, capacity difference and output voltage

Conclusion

Basic effect library:

- ◆ constructing most (electro-) mechanical devices
- ◆ controlling simulation speed and accuracy
- ◆ easy extension of the library

Implementation in VHDL-AMS:

- ◆ straightforward implementation of mathematical functions
- ◆ mixed-domain and mixed-signal modeling with *one* HDL
- ◆ system simulation becomes easy