

SOM-LS: Selective Orthogonal Matrix Least-Squares Method for Macromodeling Multiport Networks Characterized by Sampled Data

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Contents

1. Introduction
2. Selective Orthogonal Matrix Least-Squares Method
3. Macromodeling of Networks Characterized by Sampled Data
4. Examples
5. Summary



Introduction

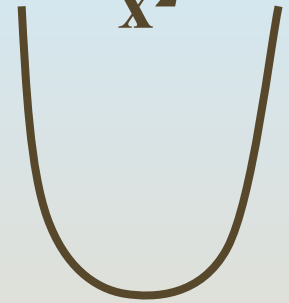
Device Model



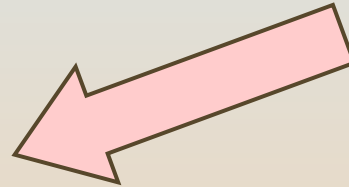
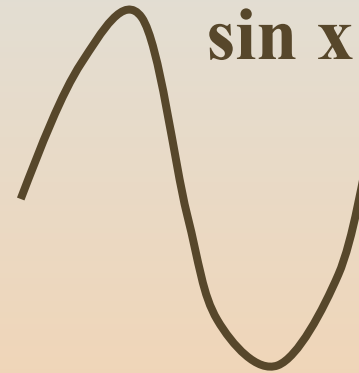
exp



x^2



sin x



Least-Squares
Fitting

❁ Which function is dominant ?



- ❁ The least-squares method for system identification **selecting the dominant basis functions** is presented.
- ❁ This method is based on a learning algorithm of neural network.
- ❁ Macromodeling of networks characterized by sampled data via electromagnetic analysis.
- ❁ The macromodels are described in the format of **Verilog-A**.

Contents

1. Introduction
2. Selective Orthogonal Matrix Least-Squares Method
3. Macromodeling of Networks Characterized by Sampled Data
4. Examples
5. Summary



Selective Orthogonal Matrix Least-Squares Method

Device Model:

$$\mathbf{G}(x) = \sum_{i=1}^N \mathbf{K}_i f_i(x)$$

\mathbf{K}_i : constant matrix

$f_i(x)$: basis function

x : design variable

- The device model is made by least-squares fitting of sampled data

Over-determined Equation:

$$\mathbf{PK} = \mathbf{F}$$

$$\mathbf{P} = \begin{bmatrix} f_1(x_1) & f_2(x_1) & \cdots & f_M(x_1) \\ f_1(x_2) & f_2(x_2) & \cdots & f_M(x_2) \\ \vdots & \vdots & \cdots & \vdots \\ f_1(x_N) & f_2(x_N) & \cdots & f_M(x_N) \end{bmatrix}$$

$$\mathbf{F} = [\mathbf{G}(x_1), \mathbf{G}(x_2), \dots, \mathbf{G}(x_N)]^T$$

- The over-determined matrix equation is solved by orthogonal least-squares method.

- ❁ The coefficient matrix is rewritten by

$$\mathbf{P} = [\mathbf{p}_1, \mathbf{p}_2, \mathbf{p}_3, \mathbf{p}_4, \dots, \mathbf{p}_k, \dots, \mathbf{p}_N]$$

- ❁ The **number of basis functions** is equal to the **number of orthogonal vectors**
- ❁ The key issue is how to select the column vectors and orthogonalize them.

$$\mathbf{P} = [\mathbf{w}_1, \mathbf{w}_2, \mathbf{w}_3, \mathbf{w}_4, \dots, \mathbf{w}_{k-1}, \mathbf{p}_k, \dots, \mathbf{p}_N]$$

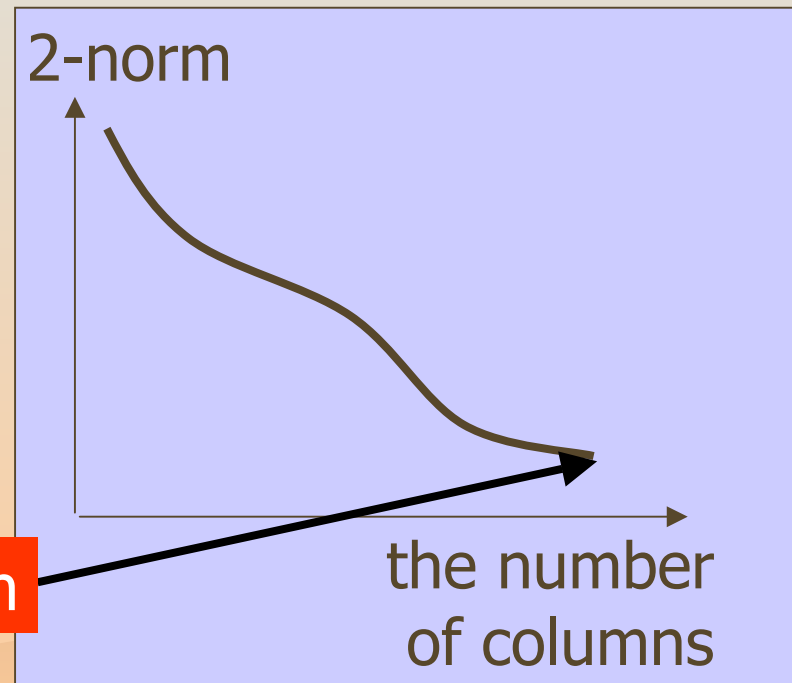
$$\mathbf{P} = [\mathbf{p}_1, \dots, \mathbf{p}_{N-k+1}, \mathbf{w}_1, \mathbf{w}_2, \mathbf{w}_3, \mathbf{w}_4, \dots, \mathbf{w}_{k-1}]$$

- After k th step in the orthogonalization, the residual matrix is defined as

$$\mathbf{Z} = \mathbf{F} - \mathbf{W}_k \mathbf{G}_k$$

\mathbf{W}_k : orthogonal matrix
 \mathbf{G}_k : intermediate solution

- The 2-norm of the residual matrix is proven to be monotonously decreasing function.

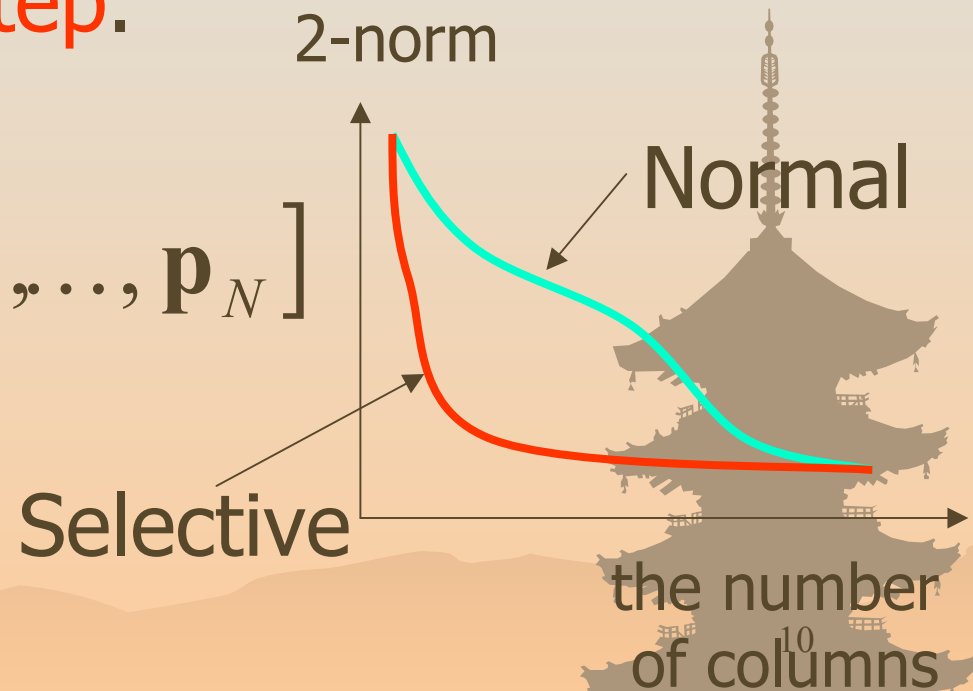


Least Squares Solution

Selective Orthogonalization

- ❁ Evaluating the 2-norm of the residual matrix, the columns of the matrix \mathbf{P} are orthogonalized so that **the 2-norm largely decreases at each step.**

$$\mathbf{P} = [\mathbf{w}_1, \mathbf{w}_2, \mathbf{p}_3, \dots, \mathbf{p}_k, \dots, \mathbf{p}_N]$$

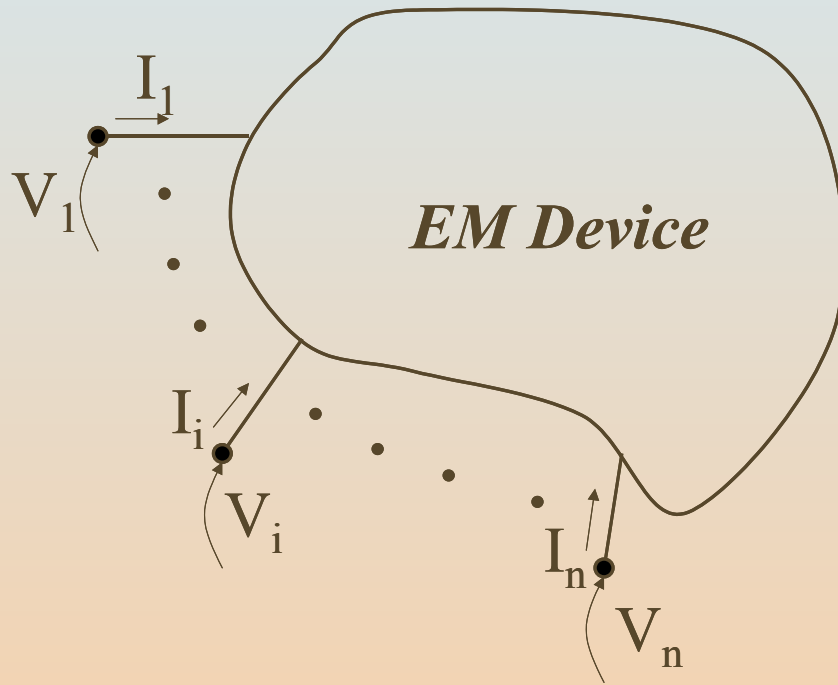


Contents

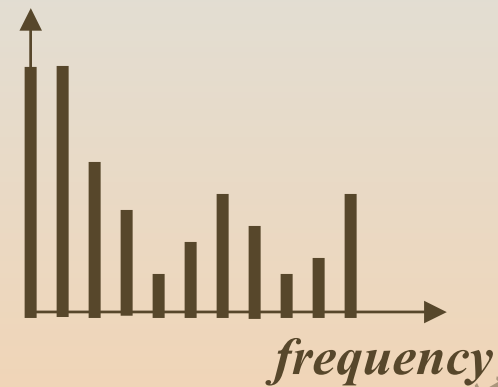
1. Introduction
2. Selective Orthogonal Matrix Least-Squares Method
3. Macromodeling of Networks
Characterized by Sampled Data
4. Examples
5. Summary



Macromodeling of Networks Characterized by Sampled Data



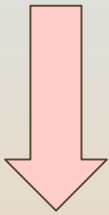
Frequency Response



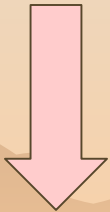
- The SOM-LS method is used for approximating the sampled data with the rational matrix.

1st Level Approximation

Sampled Data



Rational Function



Stable Poles

$$Y_{ij}(j\omega_i) = \frac{b_0 + b_1(j\omega_i) + \dots + b_m(j\omega_i)^m}{1 + a_1(j\omega_i) + \dots + a_n(j\omega_i)^n}$$

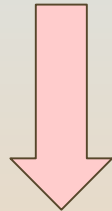
$(i = 1, \dots, N)$

Least-Squares Fitting
(scalar approximation)

Root Finding

2nd Level Approximation

Sampled Data



Rational Matrix

$$\sum_{l=1}^Q \frac{\mathbf{K}_l}{j\omega_i - p_l} = \mathbf{Y}(j\omega_i)$$

$(i = 0, 1, \dots, N)$

Least-Squares Method
(Matrix Approximation)

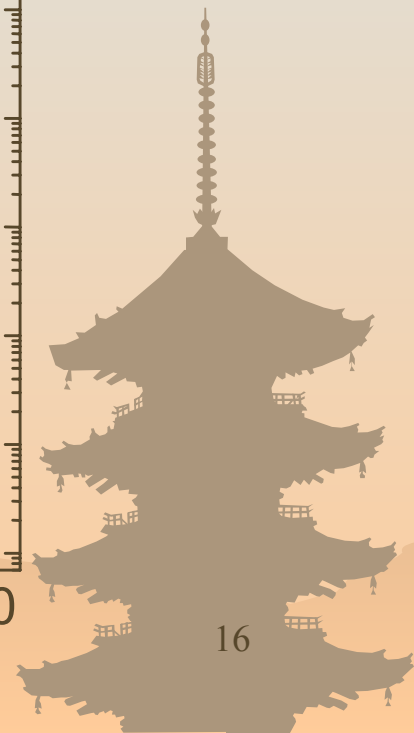
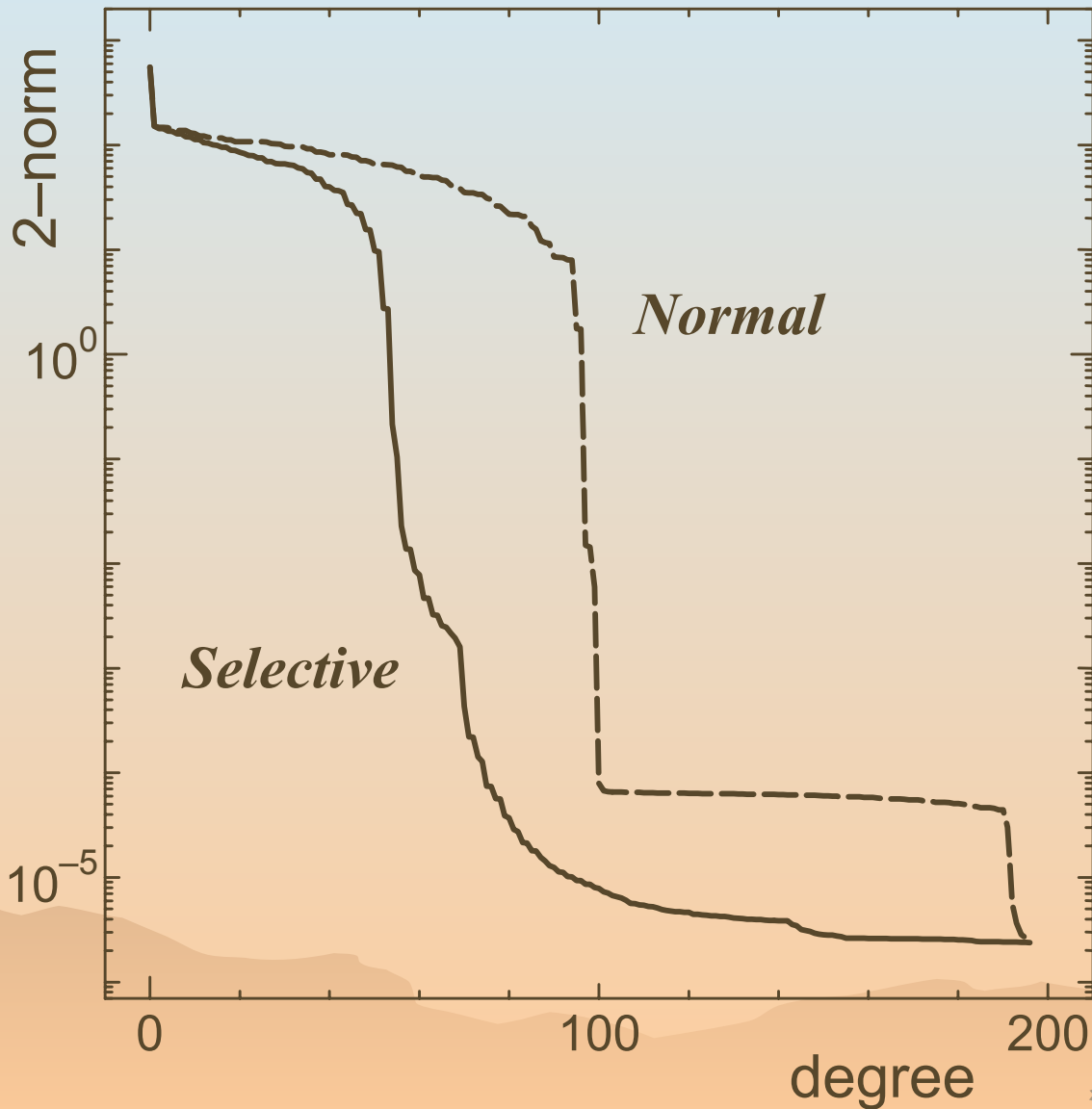
- Using the SOM-LS method, **the dominant poles are extracted** and the compact model is obtained.

Orthogonal Least-Squares Method

$$\mathbf{PK} = \mathbf{F}$$

$$\mathbf{P} = \begin{bmatrix} 1 & \frac{1}{j\omega_1 - p_1} & \dots & \frac{1}{j\omega_1 - p_Q} \\ 1 & \frac{1}{j\omega_2 - p_1} & \dots & \frac{1}{j\omega_2 - p_Q} \\ \vdots & \vdots & \dots & \vdots \\ 1 & \frac{1}{j\omega_N - p_1} & \dots & \frac{1}{j\omega_N - p_Q} \end{bmatrix}$$

2-norm of Residual Matrix



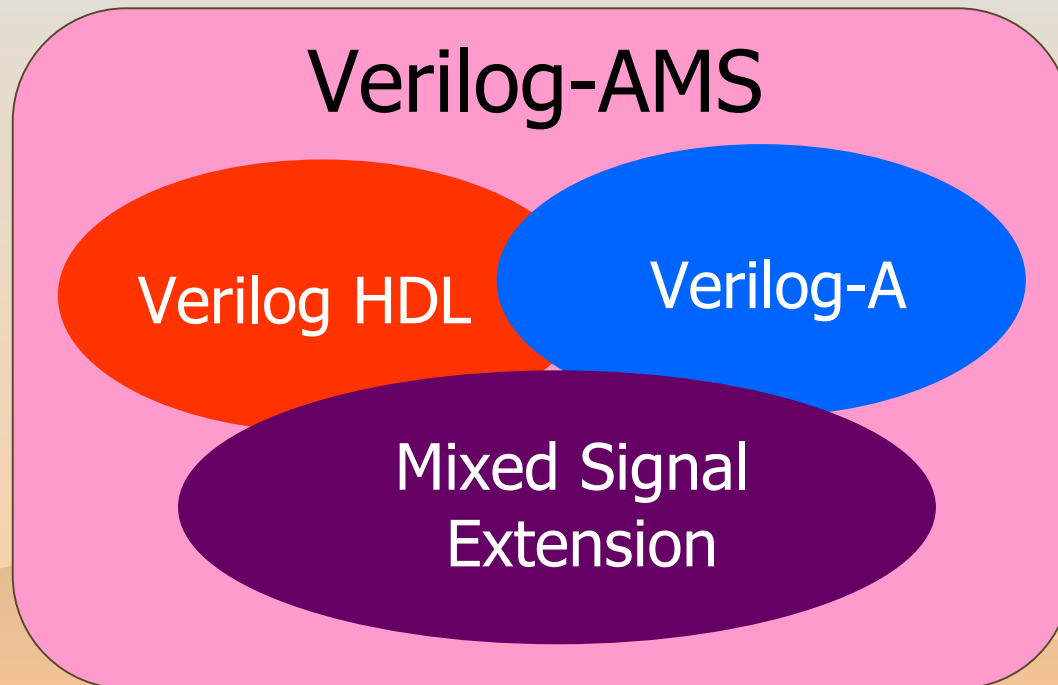
Contents

1. Introduction
2. Selective Orthogonal Matrix Least-Squares Method
3. Macromodeling of Networks Characterized by Sampled Data
4. **Examples**
5. Summary



Examples

- ❁ The macro models are described by Verilog-A.



Laplace Transform Description by Verilog-A

$$\left. \begin{aligned} V_{out}(s) &= H(s) \cdot V_{in}(s) \\ H(s) &= \frac{b_0 + b_1 \cdot s}{a_0 + a_1 \cdot s + a_2 \cdot s^2} \end{aligned} \right\}$$

```
module transfer_func(in, out);
```

```
inout in, out;
```

```
electrical in, out;
```

```
analog begin
```

```
    V(out) <+ laplace_nd(V(in), [b0,b1], [a0, a1, a2]);
```

```
end
```

```
endmodule
```

Verilog-A Model Generation

```
pole-1(real) pole-1(imag) residue-1(real) residue-1(imag)  
pole-2(real) pole-2(imag) residue-2(real) residue-2(imag)
```

:

```
module model_name(in, out);
```

```
inout in, out;  
electrical in, out;
```

```
analog begin
```

```
    V(out) <+ laplace_nd(V(in), [b0,b1], [a0, a1, a2]);
```

```
    V(out) <+ laplace_nd(V(in), [b0,b1], [a0, a1, a2]);
```

:

```
    V(out) <+ laplace_nd(V(in), [b0,b1], [a0, a1, a2]);
```

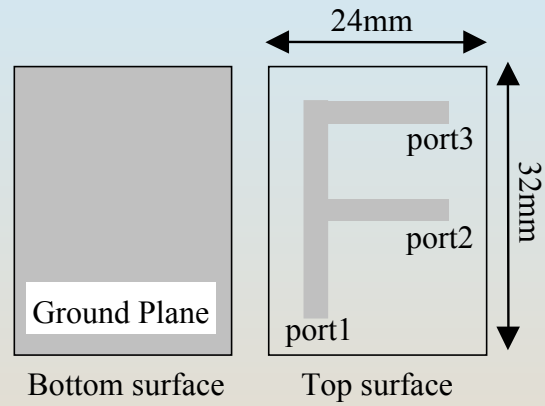
```
end
```

```
endmodule
```

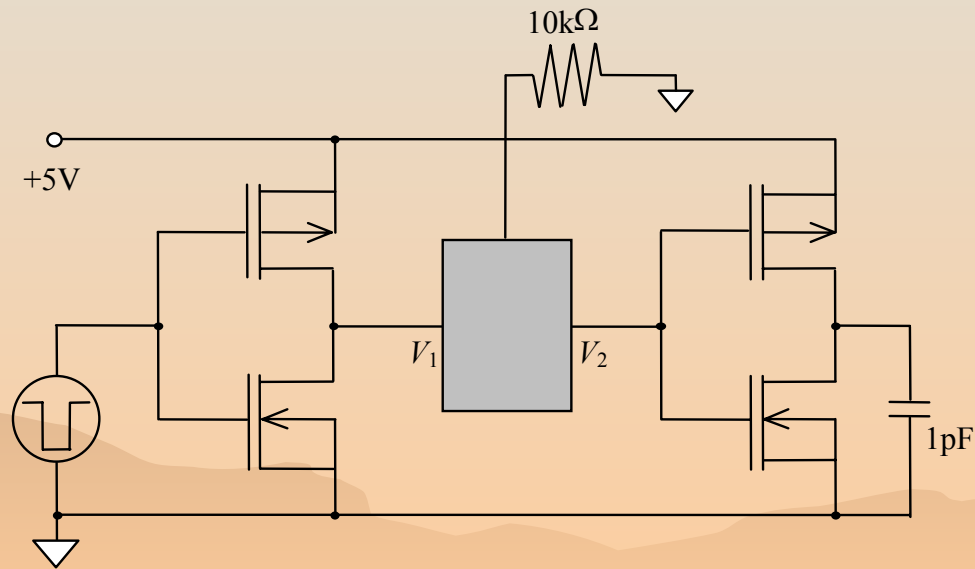
- ❁ We computed the responses of simple PCB models using *Cadence Spectre*.
- ❁ The results using the proposed macromodels were compared with the FDTD method on *Spectre*.
- ❁ The computational speed with the proposed macromodels is two magnitudes faster than the FDTD method on *Spectre*.



Example PCB Model

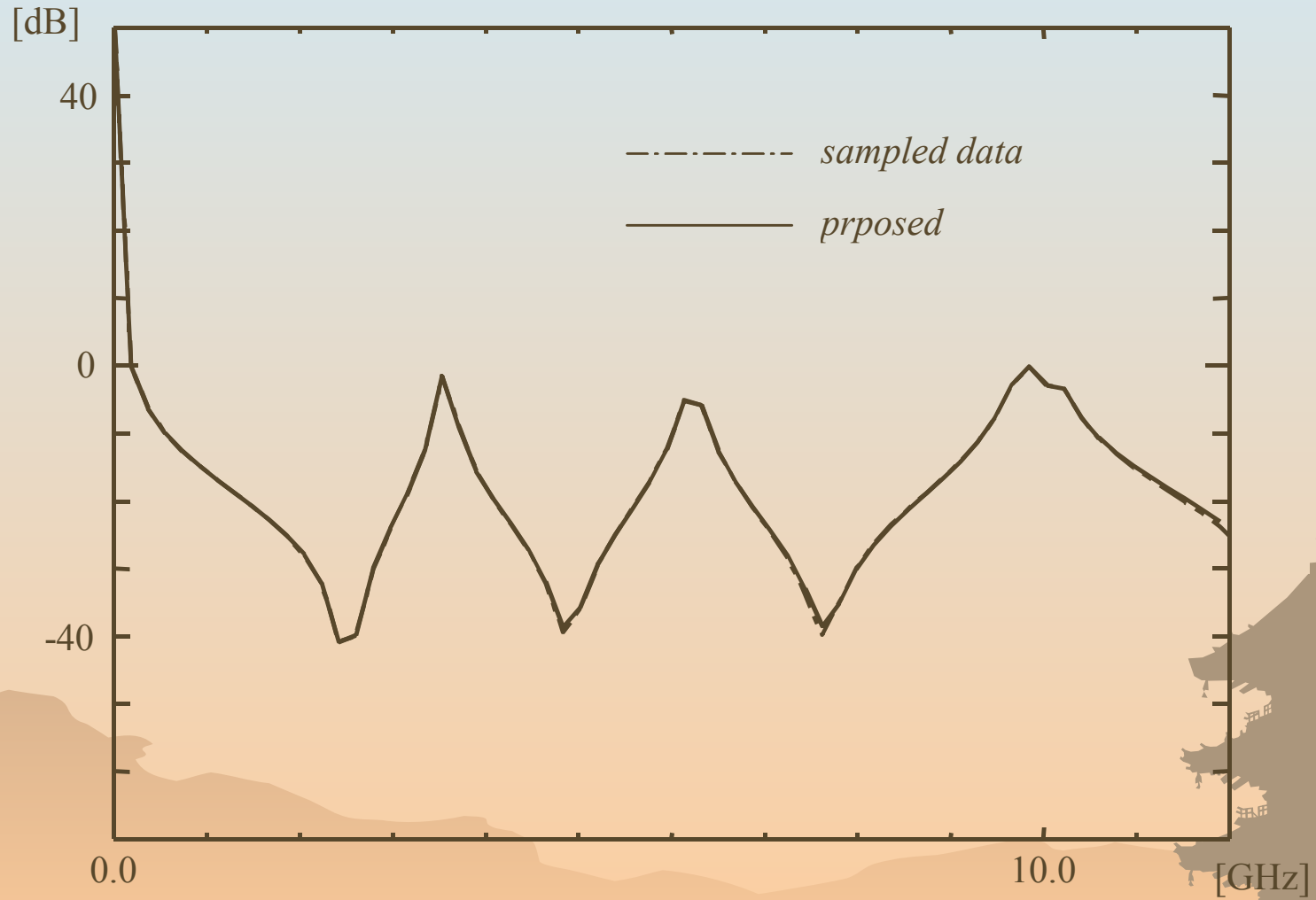


(a)

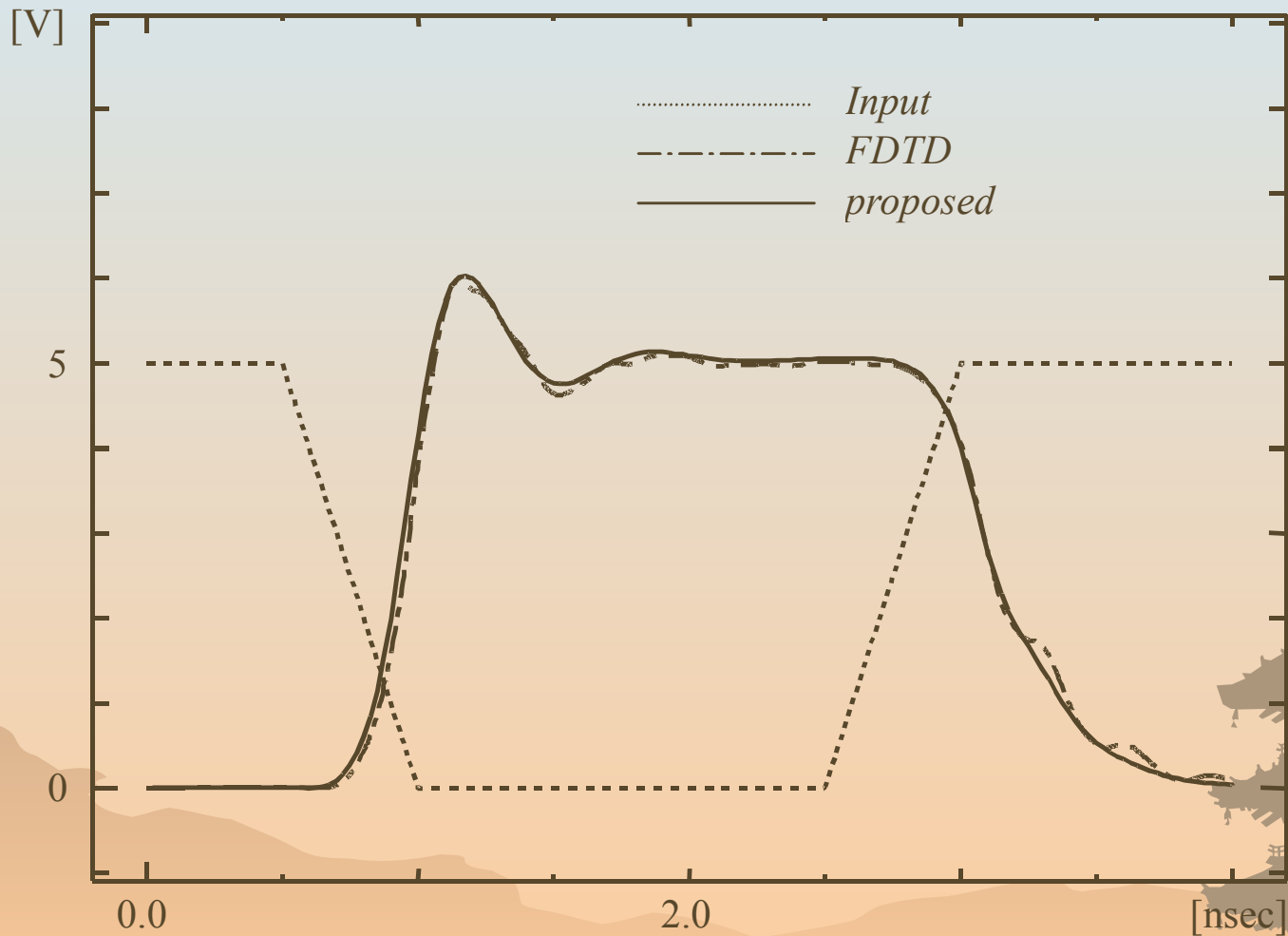


(b)

Frequency-Domain Response



Time-Domain Response



CPU Time Comparison

	FDTD	Proposed Model
Example1	550.94 (sec)	4.27 (sec)
Example2	596.19 (sec)	5.96 (sec)
Example3	416.96 (sec)	4.09 (sec)

Summary

- ❁ The selective orthogonal matrix least-squares method is presented.
- ❁ This method is applied to macromodeling of networks characterized by sampled data.
- ❁ The proposed models are described in the format of Verilog-A.
- ❁ Future work: Passivity consideration of the macromodel.